

Análise de Força Cortante em Vigas Protendidas Sem Estribo Com Uso de Concreto com Fibras:

Segundo a base de dados elaborada com ensaios disponíveis na literatura em comparação com normas internacionais.

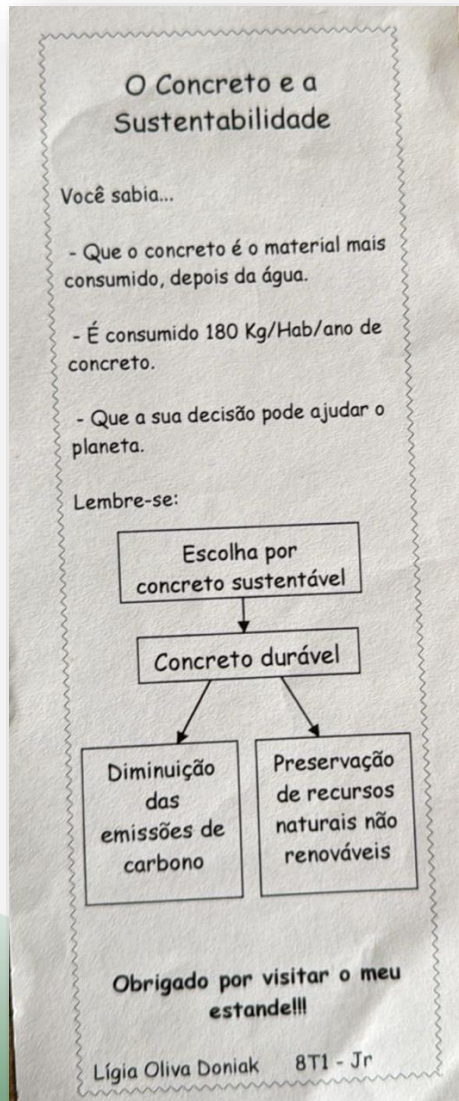
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INTRODUÇÃO

POR QUE USAR CONCRETO COM FIBRAS?

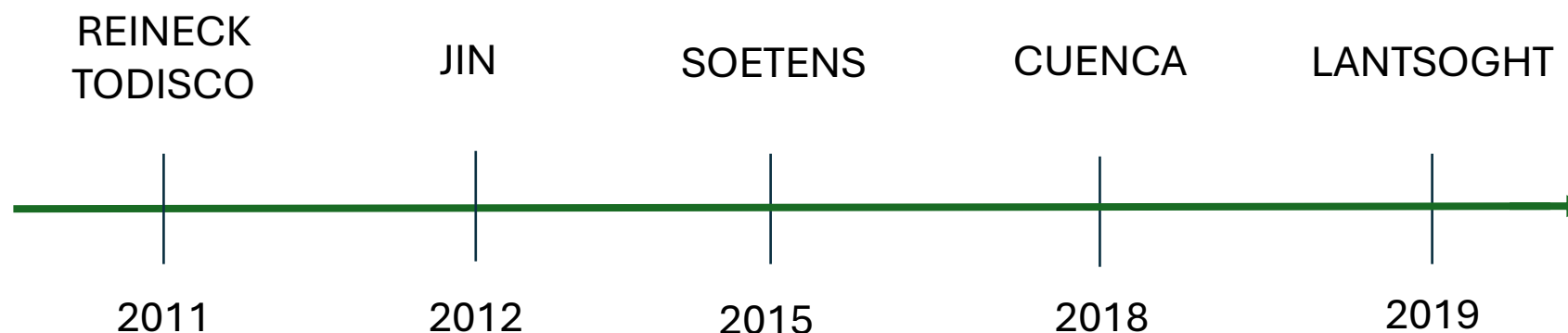
POR QUE O FRC É UMA ALTERNATIVA SUSTENTAVEL?

COMO SUBSTITUIR ARMADURA TRADICIONAL POR FIBRA?



INTRODUÇÃO

- Concreto protendido com fibra tem um alto interesse econômico e sustentável;
- É necessário conhecer bem seu desempenho e mecanismos de ruptura;
- Base de dados anteriores em resistência a cortante;



APRESENTAÇÃO DA BASE DE DADOS

DATA COLLECTION FILE: TEST

- Informação geral
- Propriedades seção transversal
- Carregamento e geometria
- Fibras e agregados
- Protensão
- Força Axial
- Resistencia do concreto
- Ensaio

DATA COLLECTION FILE: CONCRETE MIX DESIGN

- Informação Geral
- Traço
- Agregados
- Cimento
- Adição
- Pre-blended mix
- Água
- Aditivos
- Relação A/C
- Fibra

DATA EVALUATION FILE

- EUROCODE (draft)
- MODEL CODE 2010
- MODEL CODE 2010 (SMCFT)
- MODEL CODE 2020
- CODIGO ESPANHOL



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4 e 5 de junho de 2025

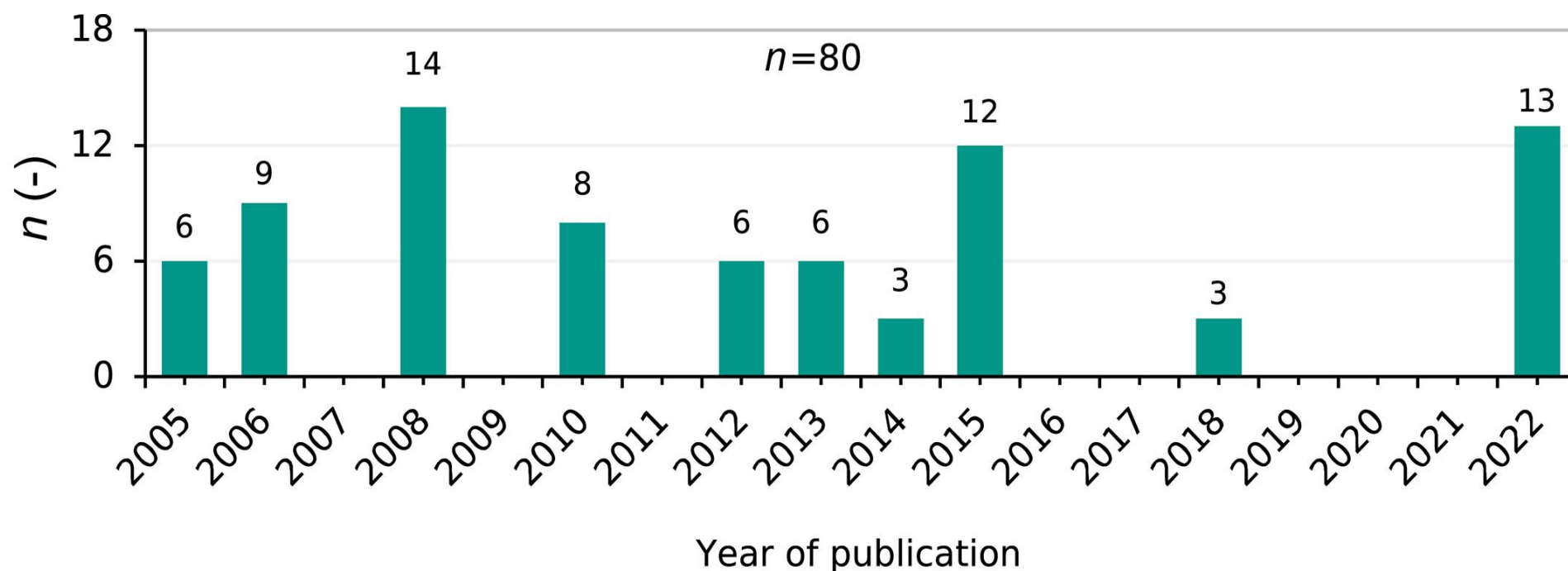
APRESENTAÇÃO DA BASE DE DADOS

DATA COLLECTION FILE: TEST

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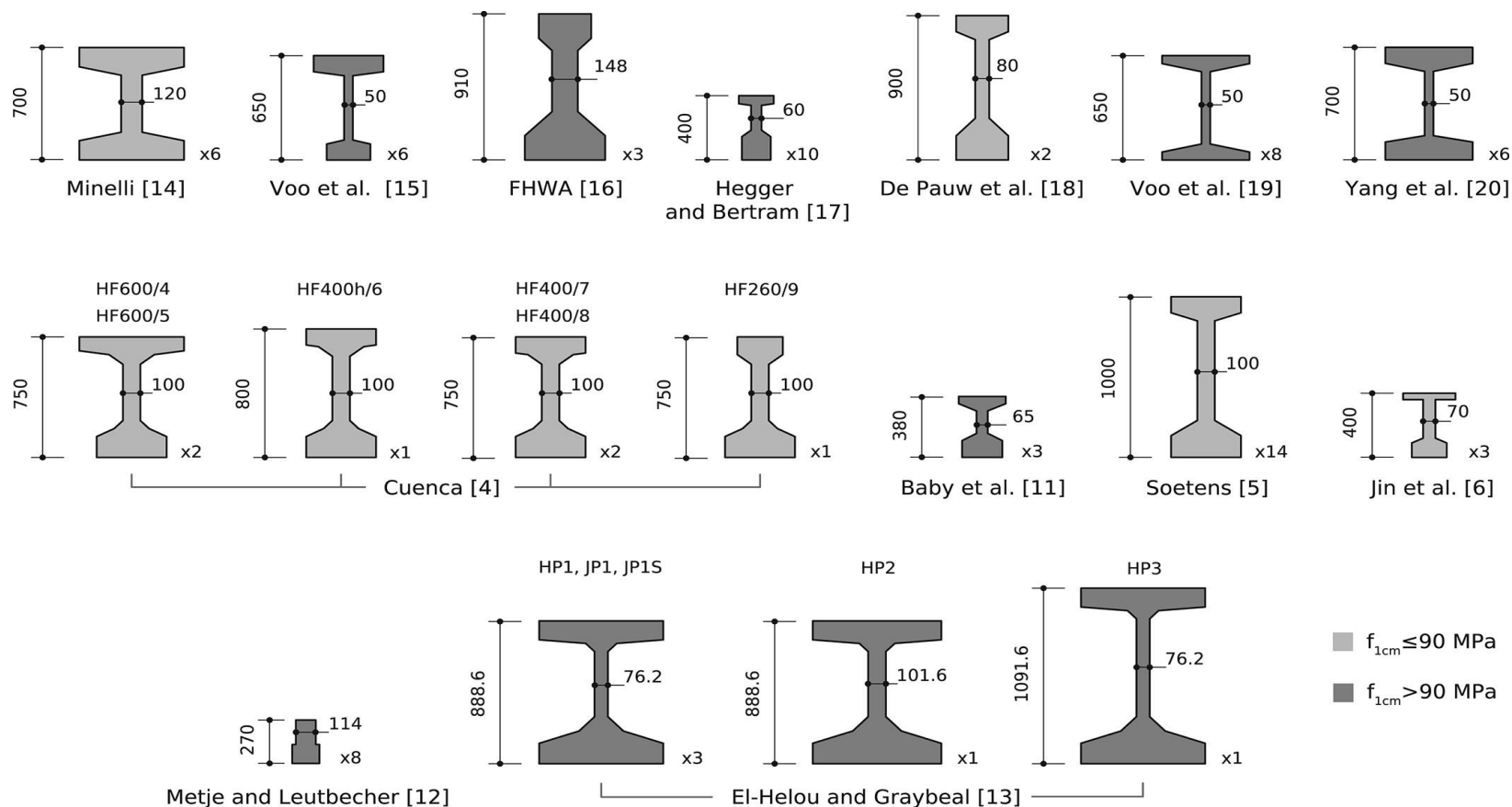
APRESENTAÇÃO DA BASE DE DADOS

Número de vigas ensaiadas pelo ano de publicação:



APRESENTAÇÃO DA BASE DE DADOS

Seção Transversal e resistência das vigas ensaiadas:

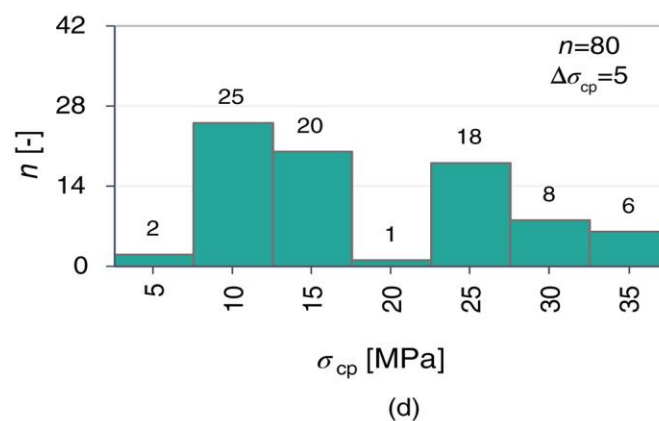
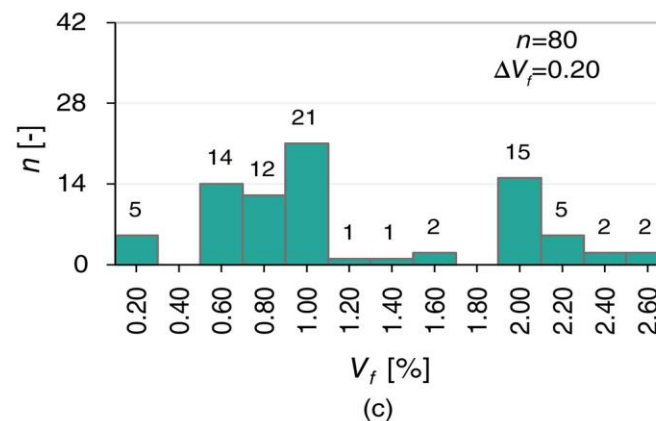
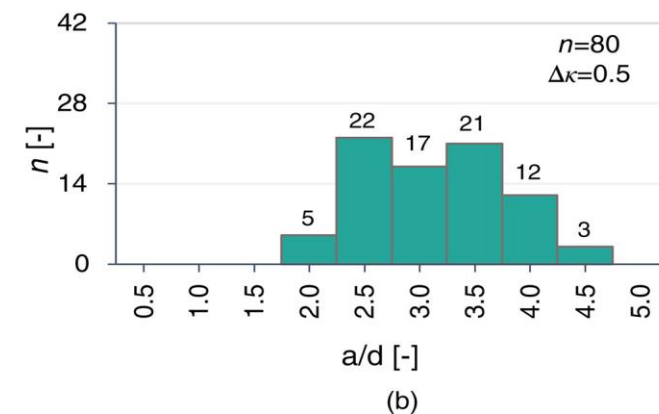
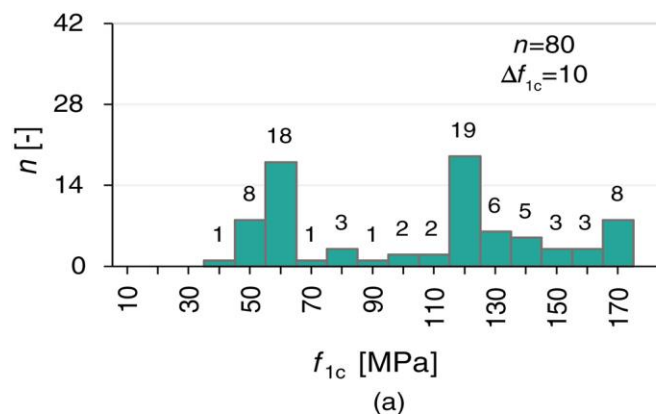


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ANÁLISE DA BASE DE DADOS

Parameter	Min value	Max value
f_{1c} (MPa)	42	175
h (mm)	270	1092
d (mm)	209	990
b_w (mm)	50	148
a/d (-)	1.75	4.50
σ_{cp} (MPa)	6.54	35.80
V_f (%)	0.30	2.50
ρ_{pw} (%)	1.00	7.59
D_{Max} (mm)	0.4	32.0
l_f/d_f (-)	48	157
σ_{fu} (MPa)	1225	3000

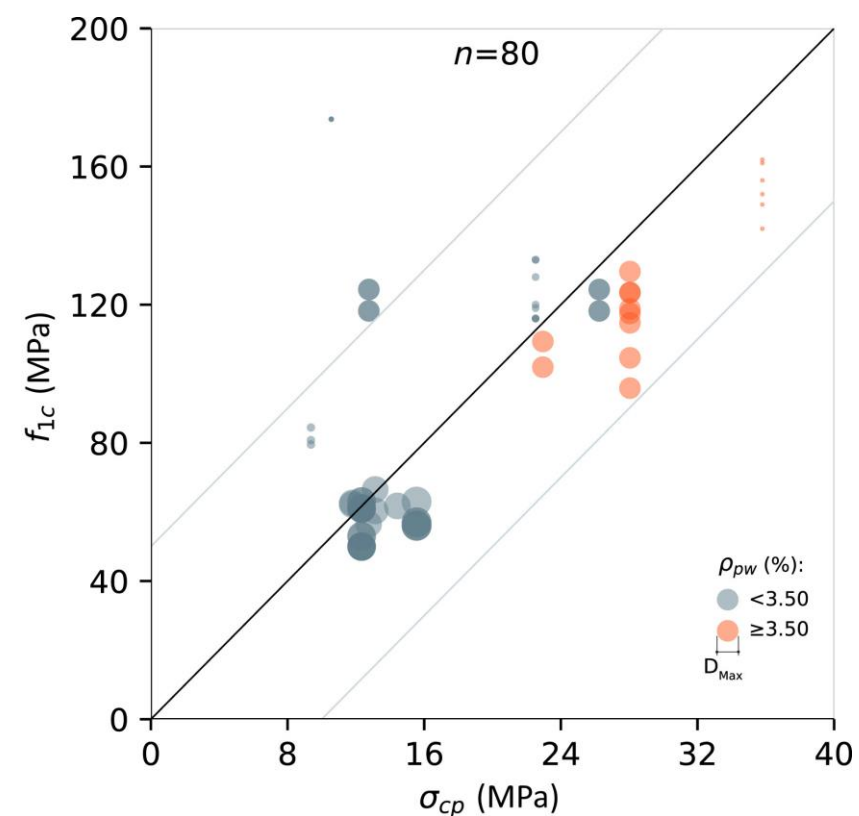
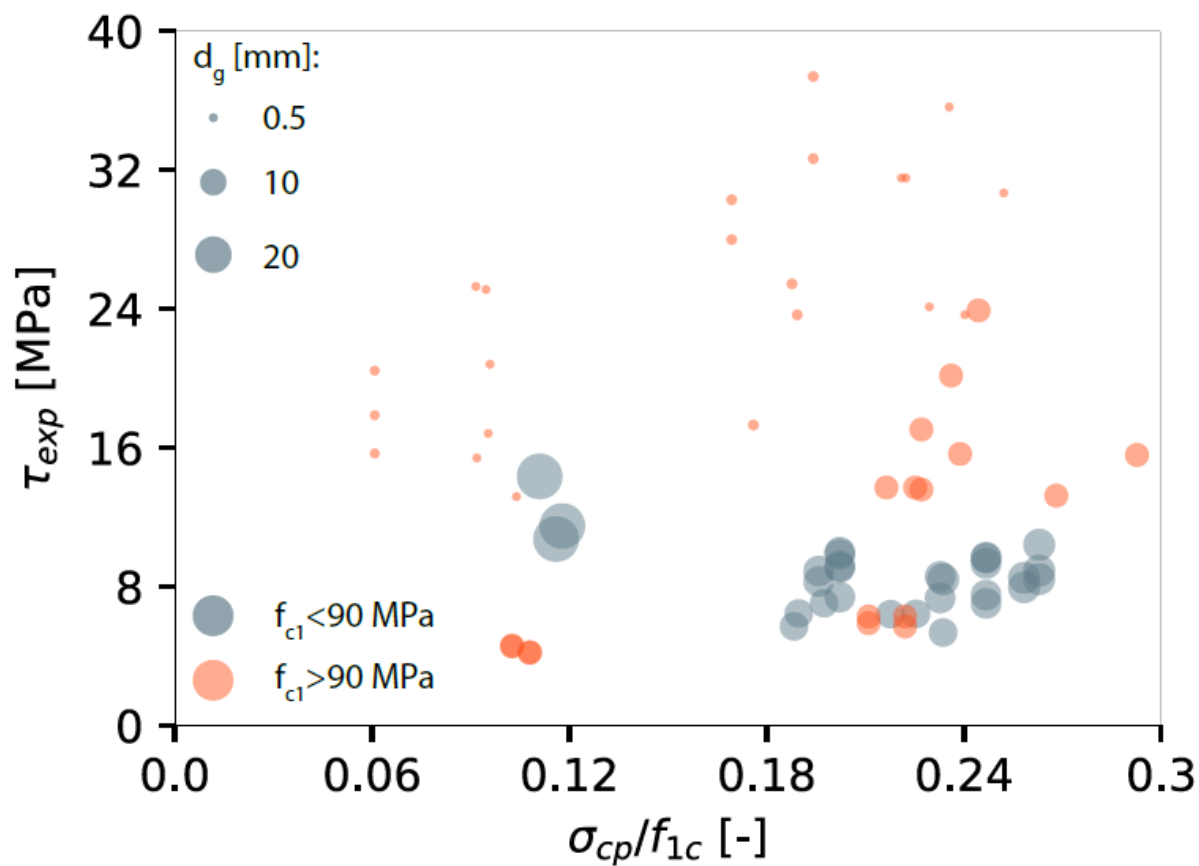
Intervalo dos parâmetros da base de dados



Número de vigas versus a. altura da viga b. esbeltez a cortante c. Resistencia a compressão do concreto d. tensão de compressão do concreto devido à protensão.

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ANÁLISE DA BASE DE DADOS



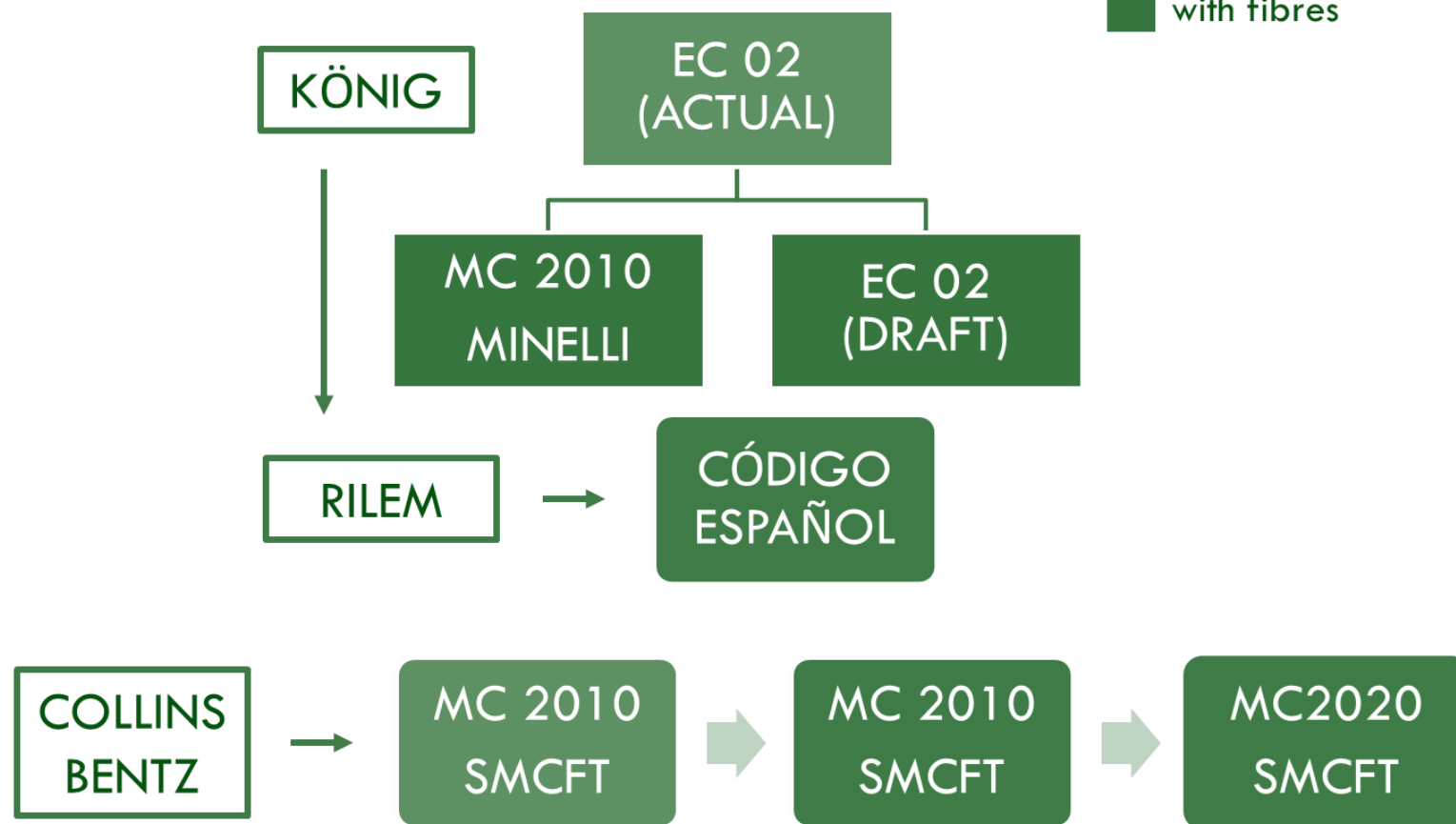
FORMULAÇÕES

FORMULA AND ORIGINS

Shear formulations:

■ without fibres

■ with fibres



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FORMULAÇÕES

EUROCODE (DRAFT):

$$V_{Rd,cf} = \left(\eta \frac{0.6}{\gamma_c} \left(100 \rho f_{ck} \frac{d_{dg}}{d} \right)^{\frac{1}{3}} + f_{Ftud} \right) \geq \eta \tau_{Rdc,min} + f_{Ftud} \Big) b_w d$$

- $f_{Ftud} = f_{Ftu, \text{rígido}} = f_{R3}/3$
- $f_{ck} < 100 \text{ MPa}$

MODEL CODE 2010 (MINELLI):

$$V_{Rd,c} = \left(\frac{0.18}{\gamma_c} k \left(100 \rho \left(1 + 7.5 \frac{f_{Ftuk}}{f_{ctk}} \right) f_{ck} \right)^{1/3} + 0.15 \sigma_{cp} \right) b_w d$$

- $f_{Ftuk} = f_{Ftu, \text{rígido}} = f_{R3}/3$
- $f_{ck} < 120 \text{ MPa}$

CÓDIGO ESPANHOL:

$$V_{Fd} = 0.7 \cdot k \cdot \tau_{fd} \cdot b \cdot d$$

$$V_{cd} = \left(\frac{0.18}{\gamma_c} k (100 \rho f_{ck})^{1/3} + 0.15 \sigma_{cp} \right) b_w d$$

$$k = 1 + \sqrt{\frac{200}{d}} \leq 2$$

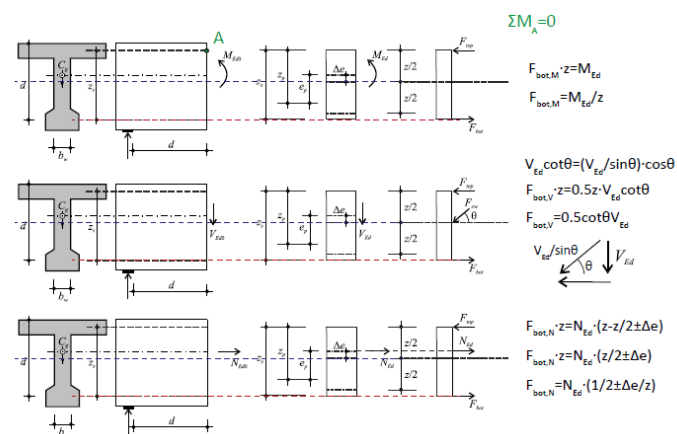
$$k = 1 + \sqrt{\frac{200}{d}} \leq 2$$

$$\tau_{fd} = 0.5 \cdot 0.33 \cdot f_{R3}$$

- $f_{ck} < 90 \text{ MPa}$

MODEL CODE 2010 (SMCFT):

$$V_{Rd,F} = \frac{1}{\gamma_F} (k_v \sqrt{f_{ck}} + k_f f_{Ftuk} \cot \theta) b_w z$$



MODEL CODE 2020:

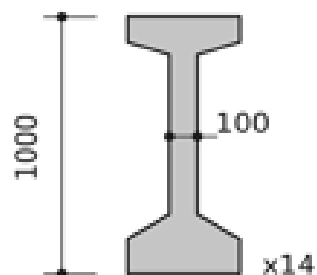
$$V_{Rd,F} = \frac{1}{\gamma_F} (k_v \sqrt{f_{ck}} + k_f f_{Ftuk} \cot \theta) b_w z$$

- $k_v = \frac{0.4}{(1 + 1500 \varepsilon_x + \xi)} \cdot \frac{1300}{1000 + k_{dg} z}$
- $\xi = (20 - 14000 \varepsilon_x) \frac{K_s f_{Ftuk}}{f_{ck}}$
- $f_{ck} < 100 \text{ MPa}$

- $k_v = \frac{0.4}{1 + 1500 \varepsilon_x} \cdot \frac{1300}{1000 + k_{dg} z}$
 - $\theta = 29 + 7000 \varepsilon_x$
 - $k_{dg} = \frac{32}{16 + d_g} \geq 0.75$
 - $f_{Ftud} = f_{Ftu, \text{rígido}} = f_{R3}/3$
 - $f_{ck} < 120 \text{ MPa}$
- $$\varepsilon_x = \frac{\left(\frac{M_{Ed}}{z} + V_{Ed} + N_{Ed} \left(\frac{z_p - e_p}{z} \right) \right)}{2 \left(\frac{z_s}{z} E_s A_s + \frac{z_p}{z} E_p A_p \right)}$$

RESULTADOS

DADOS DO ENSAIO



Soetens [5]

1-2,5-20 A

$V_{test} = 7556 \text{ kN}$

$a/d = 2,5$

$\rho_l = 1,8\%$

$\sigma_{cp} = 12,34 \text{ MPa}$

$f_{R3} = 4,09 \text{ MPa}$

$f_{1c} = 50 \text{ MPa}$

$V_{load} = 154 \text{ kN}$

EUROCODE (DRAFT):

$$V_{Rd,cf} = \left(\eta \frac{0.6}{\gamma_c} \left(100 \rho f_{ck} \frac{d_{dg}}{d} \right)^{\frac{1}{3}} + f_{Ftud} \right) b_w d \geq \eta \tau_{Rdc,min} + f_{Ftud} b_w d = 368,13 \text{ kN}$$

MODEL CODE 2010 (MINELLI):

$$V_{Rd,c} = \left(\frac{0.18}{\gamma_c} k \left(100 \rho \left(1 + 7.5 \frac{f_{Ftuk}}{f_{ctk}} \right) f_{ck} \right)^{\frac{1}{3}} + 0.15 \sigma_{cp} \right) b_w d = 167,36 \text{ kN}$$

MODEL CODE 2010 (SMCFT):

$$V_{Rd,F} = \frac{1}{\gamma_F} (k_v \sqrt{f_{ck}} + k_f f_{Ftuk} \cot \theta) b_w z = 319,3 \text{ kN}$$

MODEL CODE 2020:

$$V_{Rd,F} = \frac{1}{\gamma_F} (k_v \sqrt{f_{ck}} + k_f f_{Ftuk} \cot \theta) b_w z = 270 \text{ kN}$$

CÓDIGO ESPANHOL:

$$V_{Fd} = 0,7 \cdot k \cdot \tau_{fd} \cdot b \cdot d$$

$$V_{cd} = \left(\frac{0.18}{\gamma_c} k (100 \rho f_{ck})^{\frac{1}{3}} + 0.15 \sigma_{cp} \right) b_w d$$

$$V_u = 337 \text{ kN}$$

V_{test}/V_{calc}

2,05

4,52

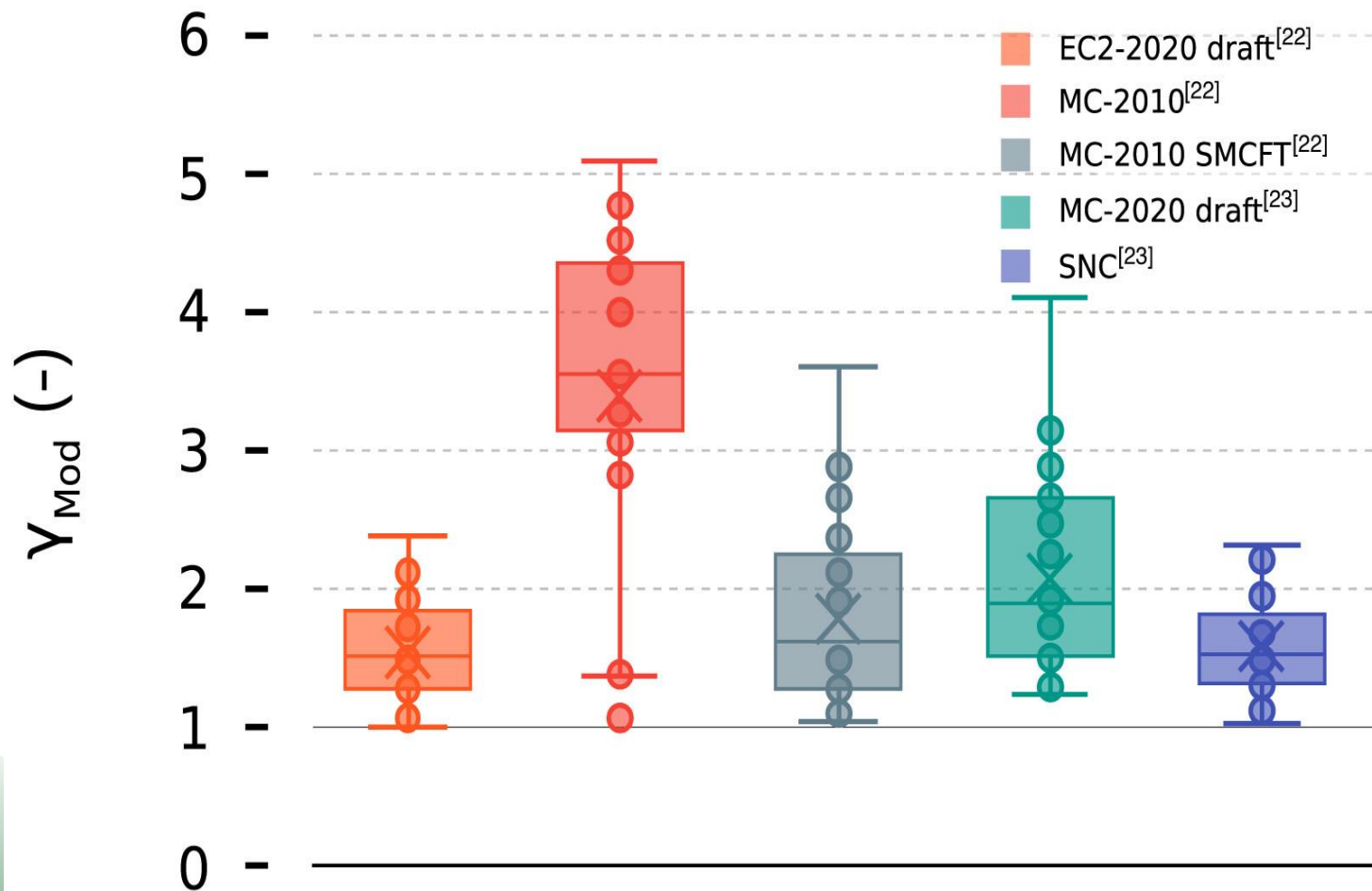
2,37

2,79

2,24

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RESULTADOS



Statistical values for γ_{mod}	EC2	SNC	MC10	MC10 SMCFT	MC20 SMCFT
n	27	26	31	31	31
m	1.54	1.59	3.39	1.78	2.07
s	0.36	0.35	1.19	0.62	0.69
$v = s/m$	0.23	0.22	0.35	0.35	0.33
$\gamma_{mod} < 1$ (%)	0	0	0	0	0

AGRADECIMENTOS



POLITÉCNICA

UNIVERSIDAD
POLITÉCNICA
DE MADRID



Colegio de Ingenieros
de Caminos,
Canales y Puertos



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Abcic
Associação Brasileira da Construção
Industrializada de Concreto

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OBRIGADA!



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